# Photon Correlation Spectroscopic Studies of Poly(vinyl acetate) above the Glass Transition Temperature

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ABSTRACT: Homodyne photon correlation spectroscopic measurements of poly(vinyl acetate) at temperatures between 31.8 and 64.5 °C have been carried out. Over this narrow temperature range, the mean relaxation time changes by more than 5 orders of magnitude. The light scattering (photon correlation) results are compared with the mechanical and dielectric relaxation data. Good agreement is found between the light scattering and the dynamic compressibility data, in support of a recent theoretical analysis.

#### Introduction

Dynamic light scattering is a useful technique for the study of relaxation processes of amorphous polymers above glass transition temperatures. By use of existing digital electronic correlators to process the scattered light, a wide frequency range from 0.1 Hz to 1 MHz can be covered. Information obtained in this frequency range is very valuable in understanding the dynamics of the glass transformation for amorphous polymers. Above the glass transition temperature  $(T_{\rm g})$ , segments of amorphous polymer chains stochastically jump from one position to another. A detailed theoretical treatment of such a type of segmental motion is very difficult, and in order to simplify the description, the free volume concept is frequently used to account for the relaxation peak observed in the viscoelastic or dielectric relaxation spectra of amorphous polymers or glass-forming liquids.

In a recent paper, we have shown, using linear response theory, that at all frequencies the dynamic light scattering spectrum arising from density fluctuations is proportional to the imaginary part of the complex longitudinal compliance. Above  $T_g$ , the shear modulus of the amorphous polymer is known to be 1 or 2 orders of magnitude smaller than the bulk modulus; thus, above  $T_{\rm g}$  the longitudinal compliance D(t) can be approximated by the bulk compliance B(t). Since bulk compliance data in the dynamic range of 1-10<sup>-6</sup> s are rarely reported in the literature, due apparently to experimental difficulty, dynamic light scattering provides a useful technique for determining the bulk compliance of amorphous polymers above  $T_{\rm g}$ . The suitability of the dynamic light scattering technique for obtaining the bulk compressibility data has recently been evaluated and compared4,5 with the dynamic compressibility data of poly(vinyl acetate) at 50 °C by Mckinney and Belcher.6

The purpose of the present work is to investigate the photon correlation spectra of poly(vinyl acetate) (PVAc) at different temperatures above but in the vicinity of the glass transition. In order to elucidate the nature of the relaxation process, we have compared the light scattering result with the mechanical and dielectric data previously published. During the course of this work, a paper dealing with dynamic light scattering of PVAc by Tribone, Jamieson, and Simha<sup>7</sup> appeared. Their results are, however,

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not in agreement with the ones presented in this paper. In a later section we discuss possible causes for the disagreement.

# **Experimental Techniques and Data Analysis**

Homodyne photon correlation functions at different temperatures (32-57 °C) are measured at a scattering angle of  $\theta = 90^{\circ}$ . The excitation light source is an argon ion laser (Lexel) operating at 5145 Å with about 400 mW of power. The depolarized scattering intensity of PVAc is small; the polarized scattering intensity was analyzed with a 28channel Malvern Loglin correlator (K7027) to obtain the single-clipped photo-count autocorrelation function  $G_k(t)$ , where k indicates the clip level. With the present log-delay correlator, the correlation function  $G_k(t)$  in a dynamic range of 4.3 decades in time (using the far-point extension) is simultaneously obtained, without the need of matching several sections of the time correlation function obtained by using different delay times in a manner similar to the method previously used. With the proper setting of delay times, the measured base line of the correlation function of PVAc at each temperature investigated is found to be equal to the calculated one, thus suggesting good quality of the measurements.

The PVAc sample used in this study was supplied through the courtesy of Dr. C. Kemenater of Wacker Chemie, Burghansen, West Germany. The viscosity-average molecular weight is  $1.5 \times 10^4$ , with an unknown molecular weight distribution. The glass transition temperature of our sample determined by DTA is low (17 °C) in comparison with the generally accepted  $T_g$  value of 29-32 °C.8 The low value obtained here is due to the low molecular weight of our sample and not due to the presence of impurity. At this molecular weight our  $T_{\sigma}$  value agrees with the literature value.9 It is interesting to note that our  $T_g$  value is similar to that of the PVAc sample used in the dynamic compressibility experiment<sup>6</sup> in which the presence of small amount of plasticizer is expected to affect the results.<sup>6</sup> Since we shall compare the light scattering result with both mechanical and dielectric relaxation data, the deviation from the conventional  $T_g$  value will not affect the interpretation, provided that the effect of different  $T_{\rm g}$  values is taken into account.

The sample used in our light scattering experiment was prepared by a procedure described elsewhere. <sup>10</sup> It is dust free and optically homogeneous. The sample displays light scattering intensity consistent with pure thermal density fluctuations, as demonstrated by the low value of the

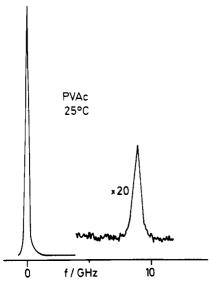


Figure 1. Rayleigh-Brillouin spectrum of poly(vinyl acetate) at 25 °C and at 90° scattering angle. The spectrum shows a low Landau-Placzek ratio.

Landau-Plazcek ratio in the Rayleigh-Brillouin spectrum. Shown in Figure 1 is the Rayleigh-Brillouin spectrum of the present sample at 25 °C at  $\theta = 90$ °. The Landau-Plazcek ratio is approximately equal to 8.

A detailed description of the method of data analysis of the measured single-clipped photoelectron-count autocorrelation function  $G_k(t)$  was given in ref 1. Here we describe only briefly the method used in the present work.

When the scattering intensity is due to density fluctuations,  $G_k(t)$  is related only to a part of the density time correlation function g(t) by

$$G_k(t) = A[1 + b|g(t)|^2]$$
 (1)

where A is the background factor which can be computed or measured by using long delay times. In the present work, the measured and computed A values agree to within 1.6% (the mean value of all correlation functions measured). The parameter b is equal to  $B\alpha_r^2$ , where B is determined by the characteristics of the correlator such as the clip levels, the delay time, and the effective photocathode area. The B factor can in principle be calculated if the spatial coherence factor of the optical system is known, but in practice, this is difficult. Thus, we determined the B factor by calibrating the optical system with pure CCl<sub>4</sub> and with a solution of polystyrene in CCl<sub>4</sub> at room temperature. The factor  $\alpha_r$  is known as the relaxation strength and it accounts for that part of density fluctuations that is detected by the correlator due to the fact that the shortest sample time of the correlator is limited to about 100 ns.

It is customary to determine the b factor by fitting the function  $[G_k(t) - A]/A$  according to some assumed function. In the present case, we assume that

$$(Gk(t) - A)/A = b \exp\{-2(t/\tau_0)^{\beta}\}$$
 (2)

treating b,  $\beta$ , and  $\tau_0$  as fitting parameters. The background factor A used is a fixed value corresponding to the measured base line and not a fitting parameter. Note in eq 2 that we have assumed g(t) to be represented by a fractional exponential, which is known to describe well the normalized correlation function g(t) with a proper set of values,  $\beta$  and  $\tau_0$ .<sup>12</sup> Here  $\beta$  is between 0 and 1.

The relaxation strength  $\alpha_r$  obtained from the fitting parameter b is calculated to be equal to 0.52, indicating

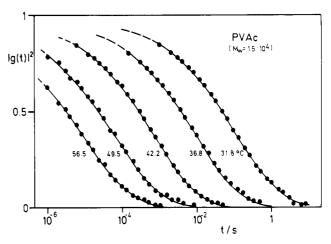


Figure 2. Normalized correlation functions  $|g(t)|^2$  determined at various temperatures plotted vs.  $\log t$ .

Table I Values of the Parameters  $\beta$  and  $\tau_0$  and Mean Relaxation Times 7 for PVAc at Various Temperatures

T/°C	β	$ au_0/\mathrm{s}$	τ/s
31.8	0.37	0.86	3.6
36.8	0.37	$6.4 \times 10^{-2}$	$2.7 \times 10^{-1}$
39.8	0.36	$1.54 \times 10^{-2}$	$7.3 \times 10^{-2}$
42.2	0.37	$4.9 \times 10^{-3}$	$2.1 \times 10^{-2}$
49.5	0.35	$4.7 \times 10^{-4}$	$2.3 \times 10^{-3}$
56.5	0.34	$4.8 \times 10^{-5}$	$4.0 \times 10^{-4}$
64.5	0.36	$1.0 \times 10^{-5}$	$4.4 \times 10^{-5}$

that only about a half of the intensity arising from density fluctuations of PVAc is probed by our correlator. The other half (48%), not accessible to the shortest time window ( $\simeq 10^{-7}$  s) of our correlator, is associated with the hypersonic wave, thermal diffusion, and fast segmental motion. All of these processes do not contribute to the time correlation function g(t), but only to the background factor A.

# Results and Discussion

The normalized correlation functions  $|g(t)|^2$  at a series of temperatures varying from 31.8 to 56.6 °C are plotted vs.  $\log t$  in Figure 2. Points represent the experimental data and the continuous curves are the fitted functions. The parameters  $\tau_0$  and  $\beta$  used to fit the time correlation functions are given in Table I. One notes in Table I that while the primary relaxation time  $\tau_0$  decreases rapidly with increasing temperature, the shape parameter  $\beta$  remains unchanged, equal approximately to 0.36-0.37 for T between 31.8 and 64.5 °C. The shape parameter is a measure of the width of the distribution of relaxation times. Constancy in the shape parameter is a good indication that only one type of relaxation process is manifested in g(t)over the temperature range studied. 11

Despite the distribution of relaxation times, it is useful to characterize the dynamic data by a mean relaxation time  $\bar{\tau}$  given by

$$\bar{\tau} = \int_0^{\infty} dt \, \exp\{-(t/\tau_0)^{\beta}\} = \tau_0/\beta \Gamma(1/\beta)$$
 (3)

where  $\Gamma(1/\beta)$  is the gamma function. The mean relaxation times computed by using the  $\beta$  and  $\tau_0$  values are also given in Table I at various temperatures. The results for  $\bar{\tau}$  are also shown in Figure 3. Over the temperature range 31.8–69.5 °C, the temperature variation of  $\bar{\tau}$  does not follow the Arrhenius equation with a constant activation energy. We now compare the present light scattering results with those of previous studies. In ref 7, Tribone et al. used a

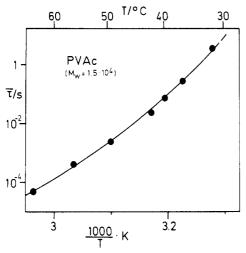


Figure 3. Mean relaxation time  $\bar{\tau}$  is plotted as a function of temperature in an Arrhenius manner.

linear correlator to collect autocorrelation function data with different sample time segments. They then matched overlapping segments to obtain a composite autocorrelation function covering five to seven decades in time. In this manner, they obtained a composite autocorrelation function described by eq 2. However, their  $\beta$  value is 0.45, considerably higher than our 0.36-0.37 value. The quoted  $\tau_0$  value at 39.3 °C is also larger than ours. When their photon correlation results are compared with the mean retardation times for volume compliance, a disagreement is found, the volume compliance data being longer by at least more than 2 orders of magnitude. This is in contrast to the present result in which we have found that the retardation time for volume compliance is in good agreement with that of the photon correlation data. Recently an elaborate analysis involving first numerically calculating the retardation spectrum from the time correlation function obtained from dynamic light scattering and then using the retardation spectrum to calculate the real and imaginary parts of the dynamic compliance in PVAc has yielded a good agreement.

It appears that the data reported by Tribone et al. need to be corrected. The origin of their difficulty may arise from improper data processing dealing with matching the correlation functions. As discussed in ref 1, although this is a necessary step in dealing with amorphous polymers, great accuracy must be obtained when measuring each section in order to be able to obtain an accurate composite time correlation function for subsequent data analysis.

We have fitted  $\bar{\tau}$  values are various temperatures to the WLF equation 13

$$\log \bar{\tau} = \log \bar{\tau}_{g} - \frac{C_{1}(T - T_{g})}{C_{2} + (T - T_{g})}$$
 (4)

where  $\bar{\tau}_g$  is the mean relaxation time of PVAc at the glass transition temperature and  $C_1$  and  $C_2$  are the parameters.

To determine the  $C_1$  and  $C_2$  values, it would be useful to plot  $(T-T_g)/\log{(\bar{\tau}/\bar{\tau}_g)}$  vs.  $T-T_g$  and then to derive the parameters  $C_1$  and  $C_2$  from the slope and the intercept of the plot. Unfortunately,  $\bar{\tau}_g$  is too long to be determined experimentally. Furthermore (as shown in Table I),  $\bar{\tau}$  changes by more than 5 orders of magnitude in a fairly narrow temperature range (about 33 °C). It is difficult to determine with accuracy the parameters  $C_1$  and  $C_2$  with the usual technique, which involves using several trial  $\bar{\tau}_g$  values until a linear plot of  $(T-T_g)/\log{(\bar{\tau}-\bar{/}\tau_g)}$  vs.  $T-T_g$  is accomplished. However, considering the fact<sup>2,4</sup> that above  $T_g$  the time correlation function g(t) essentially

reflects the time dependence of the bulk compliance B(t), we taken  $C_2 = 52$  K, as deduced from the mechanical shift factor reported in ref 6; and we then obtain, from the presently determined temperature-dependent  $\bar{\tau}$  data, log  $\bar{\tau}_g(s) = 4.6$  and  $C_1 = 18.8$  K. This gives the product of  $C_1$  and  $C_2$  to be equal to 977.6.

From the above  $\bar{\tau}_g$ ,  $C_1$ , and  $C_2$  values we obtain the Vogel-Fulcher-Tammann (VFT) equation for  $\bar{\tau}$  as

$$\bar{\tau} = \bar{\tau}_0 \exp\{B/(T - T_0)\} \tag{5}$$

where  $B=2.303C_1C_2=2252$  K,  $T_0=238$  K, and  $\bar{\tau}_0=6.4\times 10^{-15}$  s.

The VFT equation may be interpreted in terms of the free volume theory of Cohen and Turnbull. In this theory,  $T_0$  is the fictitious temperature at which the free volume for molecular motion disappears, and in the free volume theory, the parameter B given in eq 5 is equal to  $\gamma v^*/\alpha \bar{v}_{\rm m}$ , where  $\bar{v}_{\rm m}$  is the mean volume of the polymer segment responsible for the relaxation,  $\alpha$  is the thermal expansion coefficient, and  $v^*$  is the minimum required volume of the void. Taking  $\alpha = 5.8 \times 10^{-4}~{\rm K}^{-1}$ , we obtain  $\gamma v^*/\bar{v}_{\rm m} \simeq 1.31$  using  $B = 2252~{\rm K}$ . This would be contrasted to  $\gamma v^*/\bar{v}_{\rm m} = 0.95$ , obtained from a dielectric relaxation study. Since the free volume for molecular motion is equal to  $\alpha \bar{v}_{\rm m} (T-T_0)$ , it suggests that the free volume needed for density fluctuations is considerably less than that for dielectric relaxation, a result that might have been intuitively expected.

It is useful to compare the light scattering data with the mechanical and dielectric results. On the basis of reduced variables for the dynamic compressibility data, the WLF parameters  $C_1$  and  $C_2$  have been found to be equal to 17.5 and 52 K, respectively.<sup>6</sup> This is in good agreement with our light scattering data, indicating that both techniques above  $T_{\rm g}$  practically measure the same dynamic quantity and suggesting that the shear modulus makes only a negligible contribution.

The principle of reduced variables has been applied to the shear compliance data and higher molecular weight PVAc ( $T_{\rm g}=31.8~{\rm ^{\circ}C}$ ). The WLF parameters obtained from the shear compliance data are  $C_1=15.4~{\rm K}$  and  $C_2=46.8~{\rm K}$ . These values give  $B=1660~{\rm K}$ , in contrast to  $B=2096~{\rm K}$  found from the dynamic compressibility data. Thus, the free volume required for shear relaxation is also larger than that needed for density fluctuations. The WLF parameters obtained from the dielectric relaxation data of high molecular weight PVAc ( $T_{\rm g}=30~{\rm ^{\circ}C}$ ) are  $C_1=17.9~{\rm K}$  and  $C_2=43.7~{\rm K}$ , yielding  $B=1810~{\rm K}$ .

Although the physical processes that give rise to the mechanical and dielectric relaxation may be different, the closeness in the values of the parameters suggests that these methods apparently probe similar types of molecular motion, with only differences of detail as reflected by the amount of free volume needed in each case.

In descriptions of the viscoelastic data of the amorphous polymer, the dynamic modulus is often expressed in terms of the relaxation spectrum  $H(\ln \tau)$ . Here  $\tau$  is the relaxation time. As shown in ref 2 and 4, normalized time correlation functions of density fluctuations g(t) probed in the photon correlation spectroscopic experiment are related to the creep longitudinal compliance D(t) by

$$D(t) = D_0 - (D_0 - D_{\infty})g(t) \tag{6}$$

where  $D_0$  and  $D_\infty$  are the zero- and high-frequency compliance, respectively. For amorphous polymers above  $T_{\rm g}$ , we can replace the longitudinal compliance by the bulk compliance B, because the shear modulus is small.

For bulk polymers in the melt of glassy state, the shape of g(t) is complicated. Previously we approximate it as a

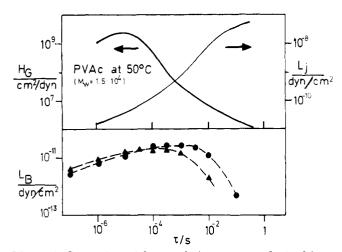


Figure 4. Comparison of the retardation spectrum obtained from light scattering data (circles) and dynamic compliance data (triangles). The retardation spectrum and relaxation spectrum constructed from the shear mechanical data reduced to 50 °C are also plotted.

fraction exponential. It is theoretically more appealing to express it as an integral sum of exponential decays taken over a distribution of relaxation times

$$g(t) = \int_0^\infty d\tau \ \rho(\tau) e^{-t/\tau} \tag{7}$$

where  $\rho(\tau)$  is a normalized distribution function.

The mean relaxation time  $\bar{\tau}$  is thus equal to the first moment of the distribution function.

$$\bar{\tau} = \int_0^\infty dt \ g(t) = \int_0^\infty d\tau \ \tau \rho(\tau)$$
 (8)

Because  $\rho(\tau)$  is normalized, we can rewrite eq 6 as

$$D(t) = D_{\infty} + (D_{\infty} - D_0) \int_0^{\infty} d\tau \ (1 - e^{-t/\tau}) \rho(\tau)$$
 (9)

Introducing the retardation spectrum  $L(\ln \tau)$ , we rewrite eq 9 as

$$D(t) = D_{\infty} + (D_{\infty} - D_0) \int_0^{\infty} d \ln \tau L(\ln \tau) (1 - e^{-t/\tau}) \quad (10)$$

where  $L(\ln \tau) = \tau \rho(\tau)$ .

The relaxation time that is determined from the photon correlation spectroscopic experiment thus represents the area of the retardation spectrum  $L(\ln \tau)$ , or the zeroth moment of  $L(\ln \tau)$  integrating over the linear scale.

One can obtain more information from the retardation spectrum itself; unfortunately, this cannot be carried out exactly at present. However, approximated methods for obtaining  $L(\ln \tau)$  exist in the literature. We use the method of Schwarzl and Staverman<sup>3</sup> to approximate  $L(\ln \tau)$ 

$$L(\ln \tau) = \left[ \frac{\mathrm{d}B(t)}{\mathrm{d}\ln t} - \frac{\mathrm{d}^2 B(t)}{\mathrm{d}(\ln \tau)^2} \right]_{t=2\tau}$$
 (11)

where B(t) is given by eq 10 (with D(t) replaced by B(t)). The retardation spectrum calculated by using this method for PVAc at 50 °C has been described elsewhere4 and is reproduced here for comparison in the lower part of Figure 4 as indicated by  $L_{\rm B}$ . The retardation spectrum calculated by using the dynamic compressibility data of ref 6 is included in Figure 4 for comparison. Except for the portion at long relaxation times ( $\tau > 5 \times 10^{-3}$  s), the

agreement between the dynamic light scattering and the dynamic compressibility techniques is quite good. The deviation at long relaxation times is probably due in part to the presence of plasticizer in the sample of ref 6 and in part to the neglect of the shear modulus, which may affect the long-time result.

The retardation spectrum constructed from the shear compliance 15 reduced to 50 °C (indicated by  $L_i$ ) is shown in the upper part of Figure 4. In reducing the shear compliance data we have taken into account the low  $T_{g}$  value of the present sample. Note that the value of  $L_i$  not only is greater than  $L_{\rm B}$  by nearly 3 orders of magnitude, but also changes by several powers of 10 over the relaxation time range of  $10^{-6}$ – $10^{-1}$  s, in contrast to the behavior of  $L_{\rm B}$  which is quite flat. Since the maximum shear compliance decreases with an increasing number of polymer molecules per unit volume, vis., L<sub>j</sub> is an increasing function of the molecular weight, it is not unexpected to see that  $L_i$  and  $L_{\rm B}$  for PVAc behave differently. As a matter of fact, it is now known that localized segmental motion is responsible for the relaxation of the bulk compliance; the bulk retardation spectrum  $L_{\rm B}$  is insensitive to changes in the longrange molecular configuration or contour shape. We expect no striking difference between polymers at low and high molecular weights in  $L_{\rm B}$ .

The relaxation spectrum  $H_G$  for the shear modulus of PVAc is also included in Figure 4. Note the maximum in  $H_{\rm G}$  occurs at shorter times than that in  $L_{\rm i}$ . This is consistent with the comparison of the maximum position of the loss longitudinal modulus and loss longitudinal compliance recently calculated by Wang and Stuhn<sup>16</sup> from photon correlation data for poly(propylene glycol). It may be pointed out that Saito has observed a similarity between his dielectric data and the viscoelastic data of amorphous polymers presented in terms of the dynamic modulus.8 Since the frequency at which the loss compliance is maximum is lower than the frequency of maximum modulus, the dielectric relaxation time is expected to be shorter than the light scattering relaxation time or the mechanical retardation time when compared at the same temperature. This observation is consistent with what has been found in PVAc, in poly(propylene glycol),1 and in nonpolymeric glass-forming liquids such as o-terphenyl. 17 In all these systems, the dielectric relaxation times are found to be shorter than the light scattering relaxation times, in contrast to prediction based on the Debye model. These results simply indicate that the free volume required for density fluctuations is smaller than that needed for dielectric relaxation, rather than a wide distribution of relaxation times associated with the relaxation function, as incorrectly suggested by Patterson.<sup>18</sup>

In summary, we have investigated the photon correlation spectrum of poly(vinyl acetate) at different temperatures above  $T_{\rm g}$ . We have compared the light scattering data with the mechanical and dielectrical relaxation data. We have shown that similar types of localized segmental motion are probed by those techniques, with detailed difference reflected by the required free volume for the motion. The process of density fluctuations requires the least amount of free volume and is manifested by the shortest mean relaxation time when compared to the data obtained by various techniques at the same temperature. Good agreement is obtained when comparing the dynamic compliance and the light scattering data.

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Registry No. PVAc (homopolymer), 9003-20-7.

### References and Notes

- (1) C. H. Wang, G. Fytas, D. Lilge, and Th. Dorfmüller, Macromolecules, 14, 1363 (1981).
- (2) C. H. Wang and E. W. Fischer, J. Chem. Phys, in press.
  (3) J. D. Ferry, "Viscoelastic Properties of Polymers", Wiley, New York, 1980.
- (4) C. H. Wang, G. Gytas, and E. W. Fischer, J. Chem. Phys., in
- J. Hargenau, G. Meirer, G. Fytas, E. W. Fischer, and C. H. Wang, to be submitted for publication.
- (6) J. E. McKinney and H. V. Belcher, J. Res. Natl. Bur. Stand., Sect. A, 67A, 43 (1963).
- J. Tribone, A. M. Jamieson, and R. Simha, J. Polym. Sci., Polym. Symp., 71, 231 (1984).
- S. Saito, Kolloid-Z, 189, 116 (1963); H. Sasabe and C. T. Maynihan, J. Polym. Sci., Polym. Phys. Ed., 16, 1447 (1978).
- (9) The  $T_g$  value is consistent with that given by R. H. Wiley and

- G. M. Brauer, J. Polym. Sci., 11, 221 (1956) for PVAc with  $\bar{M}_v$  $= 1.5 \times 10^4$
- (10) G. Meier, G. Fytas, and Th. Dorfmüller, Macromolecules, 17, 457 (1984).
- (11) G. Fytas, "Physical Optics of Dynamic Phenomena and Processes in Macromolecular Systems", B. Sedlacek, Ed., 27th IUPAC Prague Microsymposium, Walter de Gruyter and Co., West Berlin, 1984
- (12) J. A. Bucaro, M. D. Dardy, and R. D. Corsaro, J. Appl. Phys., 46, 741 (1975).
- (13) M. L. Williams, R. F. Landel, and J. D. Ferry, J. Am. Chem. Soc., 77, 3701 (1955)
- (14) M. H. Cohen and D. Turnbull, J. Chem. Phys., 31, 1164 (1954). (15) N. G. McCrum, B. E. Read, and G. Williams, "Anelastic and Dielectric Effects in Polymeric Solids", Wiley, New York, 1967.
- (16) C. H. Wang and B. Stuhn, "Physical Optics of Dynamic Phenomena and Processes in Macromolecular Systems", B. Sedlacek, Ed., 27th IUPAC Prague Symposium, Walter de Gruyter and Co., West Berlin, 1984.
- (17) G. Fytas, C. H. Wang, D. Lilge, and Th. Dorfmüller, J. Chem. Phys., 75, 4247 (1981).
  (18) G. D. Patterson and C. P. Lindsey, Macromolecules, 14, 83
- (1981).

# Ultrasonic Relaxation Study of Aqueous Solutions of Poly(acrylic acid)

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ABSTRACT: In order to investigate ultrasonic relaxation processes due to segmental motions in aqueous solutions of poly(acrylic acid) (PAA), ultrasonic absorption measurements were carried out as functions of temperature, concentration of polymeric solute, molecular weight of polymers, and degree of neutralization in the frequency range from 0.8 to 180 MHz. The ultrasonic relaxation spectra show two relaxation processes. The relaxation frequencies are located at about 1.4 MHz and about 20 MHz, respectively, for the majority of solutions investigated. Both processes are ascribed to segmental motions of polymer chains. Relaxation processes due to the protolytic reaction of COOH groups in PAA are observed in the ultrasonic relaxation spectra of aqueous solutions of PAA maintained at pH 2-3. Kinetic parameters and magnitudes of volume changes associated with the protolytic reaction are roughly estimated. Site binding between polyion and counterion, Na<sup>+</sup>, gives only a slight contribution to the total ultrasonic relaxation spectrum of solutions of sodium polyacrylate compared to segmental motions. Viscous loss also contributes little to the total ultrasonic absorption in solutions of PAA.

The dynamic properties of polyelectrolytes in aqueous solutions have been investigated by a variety of methods, such as NMR,1-3 dynamic shear viscosity,4 and dielectric dispersion.<sup>5-8</sup> The ultrasonic relaxation method is also a powerful technique for investigating the dynamics of molecular processes such as conformational changes of polymer chains, protolytic reactions, and ion association processes in the time range of 10<sup>-5</sup>-10<sup>-10</sup> s. A number of ultrasonic relaxation studies have been carried out for nonionic polymer solutions by many investigators and the results are summarized in reviews. 9,10

Ultrasonic studies of polyelectrolytes in aqueous solutions have also been carried out by a few investigators. These studies are well summarized by Zana. 11,12 It was reported in one review<sup>11</sup> that there are two relaxation mechanisms associated with site binding between a polyion and counterions and with hydrogen-bond formation between COOH and COO-13,14 in the ultrasonic relaxation phenomena of aqueous solutions of poly(acrylic acid). Contributions of segmental motions and protolytic reaction to ultrasonic absorption of polyelectrolytes are neglected in the review. 11 However, it has been shown 9,10 that segmental motions give an important contribution to ultrasonic absorption in polymer solutions in the megahertz frequency range. Moreover, protolytic reaction contributes to ultrasonic absorption in monomeric carboxylic acids. 15,16 Therefore, the protolytic reaction should also be responsible for ultrasonic relaxation in aqueous solutions of poly(acrylic acid). We speculate that the frequency ranges were not wide enough and the accuracy of the data below 10 MHz was not sufficient in previous work<sup>13,14</sup> to disclose the contributions mentioned above.

In this work, accurate measurements of ultrasonic absorption of aqueous solutions of poly(acrylic acid) have been carried out over a wider frequency range and at lower concentrations than in earlier work to disclose several contributions to ultrasonic absorption such as segmental motions, protolytic reaction, and site binding between a polyion and counterions. Ultrasonic relaxation spectra of aqueous solutions of poly(acrylic acid) were obtained as functions of temperature, concentration, molecular weight, and degree of neutralization of the samples, together with the spectra of acrylic acid and sodium acrylate. Ultrasonic relaxation spectra in aqueous solutions of sodium poly-